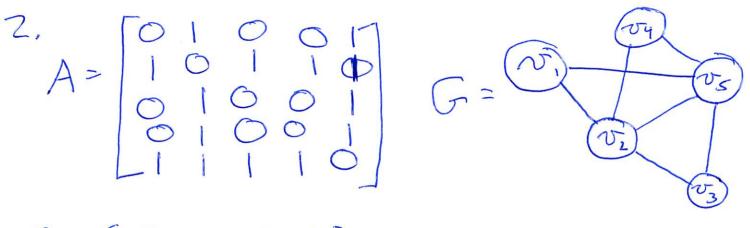


degree sequences cycle enumeration a) $\{4,3,3,2,2,2\}$ a) $\{6,5,4,4,3,3\}$ b.) $\{4,3,3,2,2,2\}$ b.) $\{6,5,5,4,3,3\}$ c.) $\{3,3,3,3,2,2\}$ c.) $\{6,5,5,4,3,3\}$ d.) $\{6,6,4,4,4,4\}$ e.) $\{3,3,3,3,2,2\}$ e.) $\{6,5,4,4,4,4\}$

To show pairwise non-isomorphism, I enumerated all possible cycle lengths in each graph. Only b-c have the some cycle lengths, but they have a difference degree sequence. Isomorphic graphs will have the same subgraphs and degrees,



5 = 22, 4, 2, 2, 43

-By the above sequence, we see the graph has even d(v) to eV(G), we also see that G is connected. ... G is Everian.

-G is not bipartite because it contains an odd cycle e.g., Evy, vz, vs, vy3.
-G has a single connected comparent;

3. G= (U, E), IV/4/E/ => 3 Cm & G Base case: 8º IVI=1, IEI=1, C, EG Hypothesis: Assume for some P(k)=H wherek=|E(H)|= |V(H)|=> Cm & H Inductive Step: Consider graph G where P(n)=G, k = n=|E(G)|= |E(G)| = |V(G)|

Consider some e E E (G), we perform on edge contraction on e

this produces some graph H where IE(H) 1= IE(G) 1-1 and IV(H) = IE(G) 1-1. We invoke our I.H. on H, and assume I Cm & H. Edge contraction preserves cycles during re-expansion, so this cycle wMI also exist on G. D

4. Gis simple, connected, [E[G)]=even => 3D= EP2, P2, ..., P23, P2=0-0-0 Dase Case: 0-0-0 =7 decomposition 13 graph Hypothesis: assume for some H=P(k) where |E|=k=even, H connected, smple⇒30=£P2...} Inductive Step: Consider G, P(n)=G, k<n=IE(G) We select some orbitrary P2 & G Case 1: H=G-Pz, H is connected We mooke I.H. on H, DG= DH+PZ Case 2: H=G-Pz, His disconnected and contains all even components H, Hz (Hz) We mucke I.H. on components, OG=DH+DH2+P2 Case 3: H=G-Pz, H has two odd components

odd Pz woodd from each odd component we

H, Make them even and can then

Mucke our I, H, on them, DG=DH,-(u,a) + DHz-(w,b) + {a,u,v}+{v,wb} Note: removing two edges splits the graph Ato at most three components

5.GEG where n=odd => G is b.portite Base Case: 0-0 Hypothesis: Assume for P(k)=H where CneHin=odd => His bipartite Inductive step: Consider G= H+e, e=(u,v) Case 1: Ot-e--O edge e is added to H

between vertices existing in

H's bipartle sets B, Bz

Orport Itian on G = B, Bz Case 2: (a) e is added between vertices in B, or Bz. In order for the addition of this edge to crede B, Bz a cycle on \$G, there must exist some u, v-pathet. As u, v+B, this path would necessartly be sald even, creating an odd cycle on G which contradicts our assumption, in no such path exists and u, v are in separate components of H. Big Bz we define u's componentas B, Bz

and v's as Bz, By. When adding

by in e, we then can define G's

bypartition as [B, + By] {Bz+Bz}